# Simulating Human Saccadic Scanpaths on Natural Images

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#### **Abstract**

Human saccade is a dynamic process of information pursuit. Based on the principle of information maximization, we propose a computational model to simulate human saccadic scanpaths on natural images. The model integrates three related factors as driven forces to guide eye movements sequentially — reference sensory responses, foveaperiphery resolution discrepancy, and visual working memory. For each eye movement, we compute three multi-band filter response maps as a coherent representation for the three factors. The three filter response maps are combined into multi-band residual filter response maps, on which we compute residual perceptual information (RPI) at each location. The RPI map is a dynamic saliency map varying along with eye movements. The next fixation is selected as the location with the maximal RPI value. On a natural image dataset, we compare the saccadic scanpaths generated by the proposed model and several other visual saliency-based models against human eye movement data. Experimental results demonstrate that the proposed model achieves the best prediction accuracy on both static fixation locations and dynamic scanpaths.

### 1. Introduction

In human visual system, neurons representing different retinal eccentricities have different spatial frequency tuning. Foveal neurons have a smaller average receptive field size and are better tuned to high spatial frequencies. They are capable of processing visual information at very high spatial resolution. On the other hand, cortical neurons representing peripheral vision have larger receptive fields and are more sensitive to the lower range of spatial frequencies. They are capable of processing information at low spatial resolution [8]. So the information from a foveal image at one fixation

is very limited. Human saccadic eye movement is an important mechanism to compensate for the loss of visual acuity in the periphery and to actively pursue information around the scene. In a highly dynamic and cluttered world, to acquire visual information efficiently and rapidly, it is important for our brain to decide not only where we should look at, but also the sequence of fixations. Indeed, both of them are essential for us to understand human saccadic behavior.

In the paper, we propose a computational model to simulate human saccadic scanpaths on natural images without a particular task. Investigating this topic is not only helpful in understanding the computational aspects of visual perception, but also beneficial to many important applications such as image and video compression, object detection, and web-page design.

**Proposed method** The proposed saccade model integrates three factors that drives human attention reflected by eye movements: reference sensory responses, foveaperiphery resolution discrepancy, and visual working memory.

Fig. 1 shows the framework of the proposed model. The three modules highlighted with a grey-blue background are the key factors. (i) The reference sensory responses of an image are multi-band filter responses of sparse coding functions extracted from the stimuli. They are considered as a representation of the raw input signal and serve as the reference information in the proposed system. Neurophysiological evidence shows that the receptive fields of neurons in the primary visual cortex (V1) are similar to sparse codes

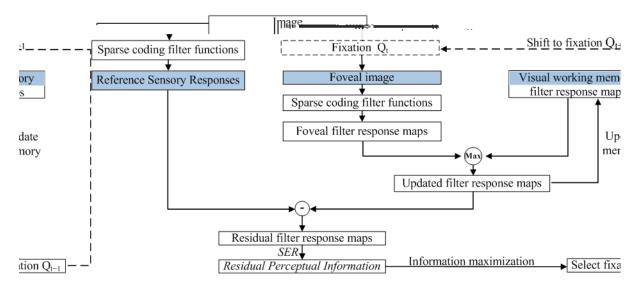


Figure 1. The proposed framework.

ter response maps of this foveal image are extracted. (iii) Visual working memory retains perceptual information for a certain period of time and inhibits immediate return of attention. We also represent the content in working memory with multi-band filter response maps. To simulate the decay of working memory, we multiply the filter response maps in the memory with a forgetting factor  $\epsilon$  ( $0 \le \epsilon \le 1$ ). We update visual working memory by taking the maximal filter response values of the foveal image filter responses and the current decayed filter responses in the memory at each location. The resulted filter responses encode the so far obtained perceptual information of the scene in brain.

Then, by subtracting the updated filter response maps in the working memory from the reference sensory responses, we obtain multi-band residual filter response maps. This simulates the dynamic interaction among the three factors along with eye movements. Consequently, we compute the Site Entropy Rate [26] on residual filter response maps to obtain a residual perceptual information (RPI) map. The resulted RPI map represents the spatial distribution of the discrepancy between the amount of information stored in brain and that contained in input stimulus. In order to pursue the maximal amount of "new" information of the scene and reduce this perceptual discrepancy, according to the information maximization principle, we choose the spot of the maximal SER value as the next fixation  $Q_{t+1}$ , and then start the next iteration.

At each eye movement, the three *multi-band filter response maps* are computed as a coherent representation for the three factors. Based on this representation and the strategical implementation of the framework, we provide experimental results to demonstrate the model's capability in simulating human saccadic scanpaths.

#### 1.1. Related work

In the literature, there are two categories of research related to modeling saccadic behavior in terms of generating scanpaths. The first category focuses on computing static visual saliency maps which describe the importance of each image location by image feature contrast or image feature rarity. Itti et al. [18] propose a biologically-plausible visual saliency model based on the center-surround contrast mechanism. By arguing that [18]'s linear model of the similarity measure on color, intensity, and orientation is inconsistent with the properties of higher level human judgement, Gao et al. [10] propose a discriminant center-surround hypothesis based on mutual information. It treats saliency detection as a classification problem, and obtains an optimal solution from the perspective of decision theory. Considering that information pursuit is the driving force behind attentive sampling, Bruce et al. [5] adopt the self-information of sparse features as a saliency measure. Harel et al. [15] propose a graph-based visual saliency model which computes the equilibrium distribution of a Markov chain on a fully-connected graph as a saliency measure. Gopalakrishnan et al. [13] extend [15]'s work and apply it in salient region detection. By analyzing the log-spectrum of natural images, Hou et al. [17] compute the spectral residual of an input image and transform the spectral residual to spatial domain to obtain the saliency map. Achanta et al. [1] propose a frequency-tuned method to detect salient regions. Itti et al. [20] propose a concept of Bayesian surprise mechanism to interpret visual attention. The "surprise" is defined as the difference between the posterior and prior distributions of beliefs of an observer over the hypotheses about the world. These models use static information to predict eye fixations, but ignore many important dynamic properties in human saccadic behaviors such as fixation order. The work of [18] adopts the principles of winner-take-all and inhibition of return to generate a scanpath out of a static saliency map. However, By comparing scanpaths generated by [18]'s model with human eye movement data, we find that this kind of static saliency model cannot predict fixation order well as shown in Section 3, which suggests that the dynamic properties should be taken into account to simulate human saccade.

The second category focuses on *dynamic* visual saliency maps during human saccade from the view of information theory. Compared with the static visual salience research, the dynamic aspect of human saccade is much less studied. Lee and Yu [19] propose an information maximization framework to explain saccadic eye movements, however, it is lack of experiments to justify their model. Inspired by the framework, Renninger *et al.* [22] simulate human saccade on novel shape silhouettes with both global and local information. Nevertheless, it is not trivial to extend this model to natural images.

There are some other studies about the effective factors of eye movement. Harding *et al.* [14] manipulate low-level image features such as luminance and chromaticity to measure the effects of these changes on human scanpaths, and compare these effects to [18]'s predicted results. Foulsham *et al.* [9] find that accumulation of scanpaths facilitates fixation prediction, and scanpaths can be explained by bottom-up guidance. Both of the work find that scanpaths generated by [18]'s strategy based on static visual saliency do not predict real human saccadic behavior well. Bahill *et al.* [2] discover that most naturally occurring human saccades are within 15 degrees of visual angle. This is a fact exploited in our model.

The rest of the paper is organized as follows. In Section 2, we introduce the details of our model. The experimental results and a new evaluation method of fixation order and fixation location are presented in Section 3. Finally, we discuss some issues of the model and conclude the paper in Section 4.

# 2. Our Approach

In this section, we introduce each component of the proposed model (shown in Fig. 1) in details and elaborate the information pursuit strategy of eye movements based on the residual perceptual information measure.

### 2.1. Coherent representation of three factors

We propose multi-band filter responses as a coherent representation for the three factors. The integration of them at each eye movement produces a dynamic saliency map, which decides the next fixation.

#### 2.1.1 Sparse coding filters

Single-unit recording evidence shows that when a natural image is presented, it only activates a small number of V1 neurons [3]. To simulate this sparse property of simple cells in the primary visual cortex, the sparse coding theory is proposed to extract the intrinsic local structure of natural images for efficient coding [21].

In this paper, we use sparse coding filter functions to compute three *multi-band filter response maps* for the reference sensory responses, fovea-periphery resolution discrepancy, and visual working memory. Specifically, Independent Component Analysis (ICA) [16] is adopted to learn a set of 1§2 color sparse filter functions from 120,000 image patches of size  $8\times8\times3$  pixels, which are randomly extracted from 1500 natural color images. Then, each filter convolves an image and generates a sub-band filter response map. 64 samples of learned color sparse bases are shown in Fig. 2.



Figure 2. 64 learned color sparse coding bases.

#### 2.1.2 Foveal imaging

To simulate the foveal imaging of human eyes, we adopt Geisler and Perry's multi-resolution pyramid method to create foveal images [12]. First, the spatial resolution (acuity) at each pixel relative to the current fixation is computed by a function of eccentricity [11]. Second, we build a multi-resolution pyramid of the original image, typically of 6 or 7 levels. Third, the desired spatial resolution at each pixel in the foveal image is computed as a weighted sum of corresponding pixel values in different layers of the pyramid. An original image and one of its foveal images are shown in Fig. 3 (a) and (b).



Figure 3. An example of foveal imaging. (a) Original image (b) Foveal image at the fixation labeled by a red cross.

#### 2.1.3 Visual working memory

Once an image location is visited by the fovea, information at that fixation is acquired. Visual working memory integrates the information across previous eye movements, meanwhile, it loses the stored information at a certain rate. This forgetting property will steer eyes moving back to previously visited salient spots when the "residual information" becomes trivial, in other words, the information at the previous fixations has been forgotten. In the following we explain the mechanism of updating the filter responses in the visual working memory.

Simulating the forgetting properties. In our model, we multiply the current filter responses in working memory with a constant forgetting factor  $\epsilon$  ( $0 \le \epsilon \le 1$ ) to simulate its forgetting property. If  $\epsilon = 1$ , no forgetting effect; if  $\epsilon = 0$ , it is memoryless. In Section 3.4, we compare simulated scanpaths under different values of  $\epsilon$ . The result shows that the forgetting property is an important factor to be modeled in simulating human saccades.

**Updating visual working memory.** Visual working memory is the place where perceptual information from current fixation and previous ones is dynamically updated.

In our model, the updating process of working memory is implemented as taking the maximal filter response values between the foveal image filter responses and the current decayed filter responses in working memory at each location. A Max operation is to simulate the transient activation in the caudal superior frontal sulcus and posterior parietal cortex when updating the attentional focus [4]. This is another key process that happens in working memory. To be specific, let  $f_k^v(x,y,t)$  and  $f_k^w(x,y,t)$  represent the k-th sub-band filter responses of a foveal image and visual working memory at time t and position (x,y) respectively. Then the updating process is as follows:

$$f_k^w(x, y, t) \leftarrow \max \left( f_k^v(x, y, t), \epsilon \cdot f_k^w(x, y, t - 1) \right). \tag{1}$$

Computing residual filter response maps. The updated filter response maps in visual working memory will interact with the reference sensory responses to predict the next fixation (see Fig. 1). Psychological evidence shows that people will shift attention when they move fixation to another point [7]. Also it is known that attention shift-away is functionally equivalent to reducing stimulus strength [6]. Therefore in our model, we subtract the updated filter responses in visual working memory from the reference sensory responses to simulate the reduction of the stimulus strength. The residual filter responses are computed as  $r_k = |f_k^o - f_k^w|$ , where  $f_k^o$  represents the k-th sub-band of the reference sensory response map.

### 2.2. Measuring residual perceptual information

From the view of information theory, a residual filter response map contains the perceptual discrepancy between the information contained in an image and that stored in brain after a series of fixations. This discrepancy is what we aim to pursue in the following eye movements.

In our model, the residual perceptual information is measured by the  $Site\ Entropy\ Rate\ (SER)\ [26]$  computed from the residual filter response maps. The  $Site\ Entropy\ Rate\ model$  adopts a fully-connected graph representation for the filter response maps to simulate the cortical neuron connectivity. Random walks are deployed on the graph to model the information transmission between neurons of the network. The site entropy rate of the random walk is proposed to measure the average information transmitted from a node to all the others. In this way, each sub-band filter response map produces a SER map. By summing up all the SER maps, the total exchanged information (measured by SER value) at each location i can be obtained as:

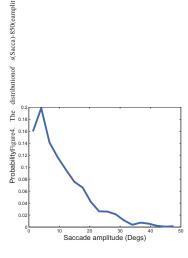
$$S_i = \sum_k SER_{ki} = -\sum_k \left(\pi_{ki} \sum_j P_{kij} \log P_{kij}\right)$$
 (2)

where  $\pi_{ki}$  is the stationary probability at location i for the k-th filter response map,  $P_{kij}$  is the transition probability of a random walk from location i to location j on the k-th filter response map. According to [26], the larger the SER value at a location is, the more salient the location is. Please refer to [26] for more details about the SER model.

There are two major reasons we adopt the SER to measure residual perceptual information. First, the SER model can explain the perceptual mechanism of the centersurround saliency whereas the residual filter response map cannot. Moreover, the residual filter response map is sensitive to noise, *e.g.*, salt-and-pepper type noise, and high frequency texture regions. Second, the residual perceptual information measure derived from SER is from the information theoretic viewpoint. This coincides with our model assumption, i.e. human saccade is a dynamic process of information pursuit.

#### 2.3. Saccadic amplitude

Using our eye movement data, we plot the distribution of saccadic amplitudes in Fig. 4. It is found that more than 90% saccade amplitudes are within  $20^\circ$  of visual angle around the current fixation point. Therefore, in the proposed model, we adopt the following randomized strategy to select the next fixation  $Q_{t+1}$  contingent on current fixation  $Q_t$ . First, a window of size  $Z\times Z$  pixles centered at current fixation point  $Q_t$  is selected, where the value of Z/2 (about 400 pixels) corresponds to  $20^\circ$  of visual angle under the eye tracking system. Then the locations where the maximal SER values inside and outside the window are selected



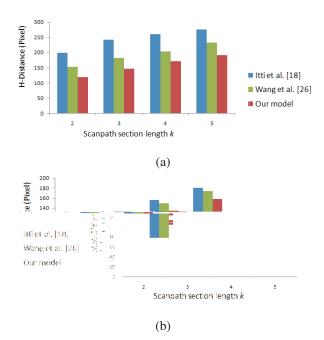


Figure 6. Comparison results between our model, [18] and [26] using Hausdorff distance (a) and mean minimal distance (b) at different scanpath length k.

### 3.2.1 Distance of scanpaths

In order to quantitatively compare the stochastic and dynamic scanpaths of varied lengths, we propose to employ time-delay embedding, which has been used widely in the study of dynamical systems [23]. Specifically, we divide scanpaths into pieces of length k, e.g.  $C_m^k(t) =$  $(c_m(t), \cdots c_m(t+k-1))$  denotes a k-dimensional timedelay embedding vector, starting at the t'th fixation generated by a model m. By varying the initial point t, the collection of all such k-dimensional vectors gives rise to the model space  $X = \{C_m^k(t)\}_t \subseteq \mathbb{R}^k$ . Similarly  $Y = \{C_h^k(\tau)\}_{\tau}$  denotes all the k-dimensional vectors in eye movement data of the same image. In particular when k=2, these vectors are discrete approximation of vector fields. Comparison between such point cloud data X and Y in  $\mathbb{R}^k$  will reflect the dynamical similarities between models and human.

For each model-generated k-dimensional vector  $x=C_m^k(t)\in X$ , define its normalized distance to the human scanpaths as  $d_k(x,Y)=\min_{\tau}\{\|x-C_h^k(\tau)\|_2\}/k$ . In other words, we search among all the length k scanpath sections of human eye tracking data on the image,  $d_k(x,Y)$  is the one with the minimum distance to the given model vector x. The smaller such a distance, the closer/more similar to human scanpath, thus a better prediction.

We use two distance measures to evaluate the scanpaths generated by a model w.r.t. human data: (i) Hausdorff dis-

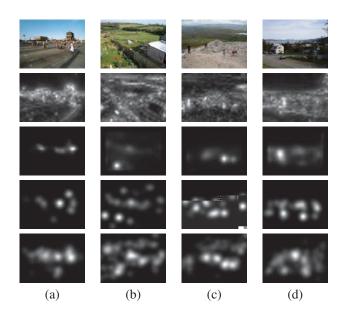


Figure 7. Comparison results about fixation density maps between our model and two other methods. The rows from top to bottom are: input images, the saliency maps by [18]'s model, [26]'s model, our model, and human fixation density maps, respectively.

tance (H-Distance) computes the maximal value of all the minimal distances between two sets of scanpaths, which is defined as

$$d_{H}^{k} = \max_{t} \{ \min_{\tau} \{ \|C_{m}^{k}(t) - C_{h}^{k}(\tau)\|_{2} \} \} / k \quad (3)$$

$$= \max_{t} \{ d_k(C_m^k(t), Y) \}. \tag{4}$$

(ii) The mean minimal distance (MM-Distance) , as its name tells, is defined as  $d_M^k = \mathrm{E_t}[d_k(C_m^k(t),Y)].$ 

In the evaluation experiments, our model parameters are set as follows: the forgetting factor  $\epsilon=0.7$ , the window size Z=800 pixels, the half-resolution of foveal imaging is  $2.3^{\circ}$ . Fig. 6 (a) and (b) show comparison results between our model and the other two methods in terms of the Hausdorff distances and the mean minimal distances, respectively. We compare scanpaths at different lengths k=2 to 5. From the comparison results, we can see that our model performs better in simulating the dynamics of saccadic scanpaths. When k>5, the distance measures increase with k due to the stochastic property of human saccadic behavior, whereas, the ranking of the compared methods remains the same. To study the individual difference in scanpaths is one of our future tasks.

## 3.3. Evaluation of fixation distribution

We compare our model with those introduced in [26] and [18] using two types of measures described in [5]: (1) the static saliency map of each image is computed as a fixation density map using a kernel-based density estimation.

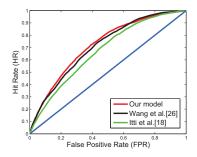


Figure 8. ROC curves of our model and two other models from [26] and [18].

Table 1. ROC area comparison

	Itti <i>et al</i> . [18]	Wang et al. [26]	Our model
ROC area	0.6706	0.7081	0.7183

Fig. 7 (a $\sim$ d) shows the comparison results. (2) We also use ROC curves and ROC areas to compare these three models in Fig. 8 and Tab. 1. Both the ROC curves and ROC areas are generated by classifying the locations in a saliency map into fixations and non-fixations with varying quantization thresholds. The larger is the ROC area, the better prediction does the model make. From both figures and the table, it can be seen that our model predicts human fixations more accurately than [18], and comparable to [26].

### 3.4. Assessment of the forgetting factor

To assess modeling the decay property of working memory, we generate a series of scanpaths on each image of the dataset by tuning the forgetting factor  $\epsilon$  from 0 (memoryless) to 1 (remember every detail) in our model. Fig.  $\P$  shows the average mean minimal distances between the simulated scanpaths and eye tracking data with different  $\epsilon$  over all the images of the dataset. Note that the results using Hausdorff distance are similar, hence, omitted. To select the optimal forgetting factor, we also compute the average distance of different saccade length k at each  $\epsilon$ . The plotted curve in Fig. 10 clearly shows that when  $\epsilon=0.7$ , the model predicts the scanpaths best.

During the experiment, we observe two interesting phenomena. (i) When  $\epsilon$  is small, e.g.  $\epsilon=0$  for an extreme case, the model quickly forgets just acquired information in working memory. As a result, the simulated scanpath will be trapped into the oscillation in between two or three fixations. In other words, in this case, there is no inhibition of return. This obviously deviates from human behavior. (ii) When  $\epsilon$  is large, e.g.  $\epsilon=1$  for an extreme case, the model retains most of the acquired information from the previous fixations in working memory. Consequently, the simulated fixations seldom returns to the visited locations. This is also not true compared to the human data. Via generating scan-

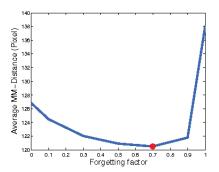


Figure 10. The average distance of different scanpath length k at each  $\epsilon$ .  $\epsilon=0.7$  is selected as model parameter.

paths under different forgetting factor and comparing them with eye tracking data, the proposed model finds the best parameter  $\epsilon=0.7$  to simulate human saccadic behavior (with fixation revisits). From both psychological evidence and the comparison results to other models, we argue that considering the forgetting effect of visual working memory plays a key role in simulating eye movements. This is one of the key differences between the proposed model and those proposed in [1§] and [22].

# 4. Conclusion, Discussion and Future Work

In the paper, we propose a computational model to simulate human saccadic scanpaths on natural images without a specific task based on the principle of information maximization. The proposed model identifies and integrates three important factors as the driving forces to guide eye movements based on a coherent multi-band sparse code filter response representation. The computational model embodies several well known psychological phenomena, such as center-surround saliency, inhibition of return, fixation revisit, algorithmic implementation of information transmission on the neural network and the forgetting effect of short term working memory, etc. We propose a new evaluation method to compare fixation order of scanpaths. Extensive experiments show the advantage of the proposed model in predicting human saccadic scanpaths.

This model is inspired by some biological evidences, but not aims to copy the exact mechanisms of visual processing. For examples, although people have different views on the accessibility of raw signal [25], the proposed model adopts the *reference sensory responses* as a reference information or knowledge to compare with the content in visual working memory and consequently guide eye movements. Also note that sparse coding may not be universally acknowledged due to its limitation in accounting for the high-order statistics of natural images, but many work still use it to represent an image because it is consistent with a lot of experimental evidence (see [24]).

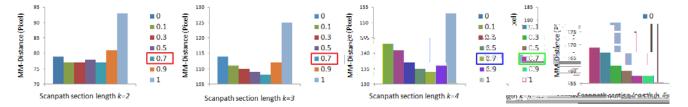


Figure 9. Average mean minimal distances between the simulated scanpaths and eye tracking data with different  $\epsilon$  over the image dataset.

In the literature, some work uses *edit distance* to measure the difference between scanpaths [\$]. We do not adopt this measure for two reasons: (i) The method introduces more free parameters, e.g. the cost for every operator. It is rather subjective to tune these parameters to make the distance measure reasonable. (ii) We observe that although there exist shared sections among scanpaths, the stochastic nature of saccade introduces much variation among scanpaths. This makes the design of operations and the operator cost tuning particular hard.

In the future, we will extend the current model to explain individual difference in scanpaths and propose some new evaluation criteria for such extension. Moreover, the fixation duration is another important attribute of saccadic behavior. It will also be considered in our future work.

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